

# ML as a Tactic Language, Again

A look at Meta-F\*

The F\* team



ML Workshop 2018



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A look at Meta-F\*

The F\* team

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# What's this $F^*$ thing?

A dependently-typed, effectful, functional programming language

- ML-like: higher-order, polymorphic, strict, safe
- Very expressive specs over effectful terms
- Proof-irrelevant logic: refinements and WP-calculus
- SMT backend (Z3)

# An example

```
let incr (r:ref int) = r := !r + 1
let f () =
  let r = alloc 1 in
  incr r;
  let v = !r in
  assert (v == 2)
```

# An example

```
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```

```
st_wp a = (state → a → prop) → state → prop
```

```
val alloc : #a:Type → x:a → ST (ref a) (λ p h → ∀r. r ∉ h ⇒ p (alloc_heap r x h) r)
val (!) : #a:Type → r:ref a → ST a (λ p h → h ∈ p ∧ p h h.[r])
val (:=) : #a:Type → r:ref a → v:a → ST unit (λ p h → h ∈ p ∧ p (upd h r v) ())
```

$$\begin{aligned}
& \forall (p: \text{st\_post\_h heap unit}) \\
& \quad (h: \text{heap}). \\
& \quad (\forall (h1: \text{heap}). \text{auto\_squash } (p \ a \ h1)) \implies \\
& \quad (\forall (a: \text{mref int (trivial\_preorder int)}) \\
& \quad \quad (h1: \text{heap}). \\
& \quad \quad \text{fresh } a \ h \ h1 \wedge \text{modifies empty } h \ h1 \wedge \\
& \quad \quad \text{sel } h1 \ a == 1 \implies \\
& \quad \quad (\forall (\text{return\_val}: \text{int}). \\
& \quad \quad \quad \text{return\_val} == \text{sel } h1 \ a + 1 \implies \\
& \quad \quad \quad \text{trivial\_preorder int (sel } h1 \ a) \ \text{return\_val} \wedge \\
& \quad \quad \quad \quad (h1: \_ : \text{heap} \\
& \quad \quad \quad \quad \quad \{\text{trivial\_preorder int (sel } h1 \ a) \ \text{return\_val}\}) \\
& \quad \quad \quad \quad \cdot \\
& \quad \quad \quad \quad \text{trivial\_preorder int (sel } h1 \ a) \ \text{return\_val} \wedge \\
& \quad \quad \quad \quad \text{contains } h1 \ a \wedge \\
& \quad \quad \quad \quad \text{modifies (singleton (addr\_of } a)) \\
& \quad \quad \quad \quad \quad h1 \\
& \quad \quad \quad \quad \quad h1 \wedge \text{equal\_dom } h1 \ h1 \wedge \\
& \quad \quad \quad \quad \text{sel } h1 \ a == \text{return\_val} \implies \\
& \quad \quad \quad \quad \text{sel } h1 \ a == 2 \wedge \\
& \quad \quad \quad \quad \quad \text{sel } h1 \ a == 2 \implies p \ \text{pure\_result } h1))
\end{aligned}$$

# Doing proofs

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- $F^*$  queries the SMT solver



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What's the modus operandi?

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- F\* computes VC
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```
val lemma_mod_spec: a:int → p:pos → Lemma (a / p = (a - (a % p)) / p)
```

# Doing proofs

What's the modus operandi?

- User writes program
- F\* computes VC
- F\* queries the SMT solver

All user input happens before VC generation: *auto-active verification*

What does the user do when then solver fails?

```
val lemma_mod_spec: a:int → p:pos → Lemma (a / p = (a - (a % p)) / p)
let lemma_mod_spec a p = ()
```

# Doing proofs

What's the modus operandi?

- User writes program
- F\* computes VC
- F\* queries the SMT solver

All user input happens before VC generation: *auto-active verification*

What does the user do when then solver fails?

```
val lemma_mod_spec: a:int → p:pos → Lemma (a / p = (a - (a % p)) / p)
```

```
let lemma_mod_spec a p =  
  lemma_div_mod a p;  
  assert (a = p * (a / p) + a % p);  
  assert (a % p = a - p * (a / p));  
  assert (a - (a % p) = p * (a / p));  
  lemma_mod_plus 0 (a / p) p;  
  assert ((p * (a / p)) % p = 0);  
  lemma_div_exact (p * (a / p)) p
```

Some proofs are just out of the solver's scope

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And the programmer's sanity scope...

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*Tactics engine*: tweak proof obligations before SMT, *interactive*<sup>1</sup> verification

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<sup>1</sup>WIP



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And the programmer's sanity scope...

*Tactics engine*: tweak proof obligations before SMT, *interactive*<sup>1</sup> verification

- User writes program
- F\* computes VC
- Custom tactics apply
- F\* *maybe* queries the SMT solver

---

<sup>1</sup>WIP

Some proofs are just out of the solver's scope

And the programmer's sanity scope...

*Tactics engine*: tweak proof obligations before SMT, *interactive*<sup>1</sup> verification

- User writes program
- $F^*$  + custom tactics compute VC
- $F^*$  *maybe* queries the SMT solver

---

<sup>1</sup>WIP

# The entrypoints

Proving:

```
... assert  $\varphi$  by  $\tau$  ...
```

Catching entire VCs:

```
let e : C by  $\tau$  = ...
```

Metaprogramming terms:

```
... ( _ by  $\tau$  ) ...
```

Metaprogramming top-level definitions:

```
%splice  $\tau$ 
```

# The entrypoints

Proving:

... `assert  $\varphi$  by  $\tau$  ...`

$\Gamma \vdash \_ : \text{squash } \tau$

Catching entire VCs:

`let e : C by  $\tau$  = ...`

$\Gamma \vdash \_ : \text{squash VC}$

Metaprogramming terms:

... `( $\_$  by  $\tau$ ) ...`

$\Gamma \vdash \_ : \text{ty}$

Metaprogramming top-level definitions:

`%splice  $\tau$`

$\cdot \vdash \_ : \text{list def}$

# Slapping a tactic on an assertion

```
let f x y z =  
  ...  
  assert (g x y == h z)  
  ...
```

# Slapping a tactic on an assertion

```
let f x y z =  
  ...  
  assert (g x y == h z)  
    by (compute ();  
        canon_semiring int_cr;  
        trefl ());  
  ...
```

# Metaprogramming: generating terms

Beyond proving, Meta- $F^*$  enables constructing terms and top-level definitions

```
let one = _ by (exact ('1))  
let one_plus_two = _ by (apply ('(+)); exact ('1); exact ('2))
```

# Metaprogramming: generating terms

Beyond proving, Meta- $F^*$  enables constructing terms and top-level definitions

```
let one = _ by (exact ('1))
let one_plus_two = _ by (apply ('(+)); exact ('1); exact ('2))

let fib (i:nat) = if i < 2 then exact ('1)
                  else begin
                      apply ('(+));
                      fib (i - 1);
                      fib (i - 2)
                  end

let t = _ by (fib 8)
```



# Metaprogramming: generating terms

Beyond proving, Meta- $F^*$  enables constructing terms and top-level definitions

```
noeq type t1 =  
  | A : int → string → t1  
  | B : t1 → int → t1  
  | C : t1  
  | D : string → t1  
  | E : t1 → t1  
  
%splice (mk_printer ('t1))
```

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noeq type t1 =
  | A : int → string → t1
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  | D : string → t1
  | E : t1 → t1

let t1_print = λv →
  let rec ff_rec v_inner =
    (match v_inner with
     | A a1 a2 →
       concat "" [ "(";
                  concat " " ["A"; print_int a1; print_string a2];
                  ")" ]
     | B a1 a2 → concat ""
                  [ "("; concat " " ["B"; ff_rec a1; print_int a2]; ")" ]
     | C → "C"
     | ...
    )
  in ff_rec v

%splice (mk_printer ('t1))
```

# Control flow

```
val f : n:int → Pure int (requires  $\top$ ) (ensures ( $\lambda n' \rightarrow n' > n$ ))
let f (n:int) =
  if n > 0
  then begin
    assert (n + n > n) by  $\tau$ ;
    n + n
  end
else 1 - n
```

# Control flow

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Context in the proofstate contains hypothesis that  $n > 0$ .

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```

Context in the proofstate contains hypothesis that  $n > 0$ .

Goal 1/1

n: int

p: pure\_post int

...

uu\_\_\_\_: squash ( $n > 0 == \text{true}$ )

-----  
squash ( $n + n > n$ )

# Extracting sub-VCs

`abstract` `with_tactic` ( $\tau : \text{unit} \rightarrow \text{Tac unit}$ ) ( $\varphi : \text{prop}$ ) : `prop` =  $\varphi$

`assert`  $\varphi$  `by`  $\tau$  : `Pure unit` (`requires` (`with_tactic`  $\tau$   $\varphi$ )) (`ensures` ( $\lambda \_ \rightarrow \varphi$ )))

- In a positive position: `with_tactic`  $\tau$   $\varphi \rightsquigarrow \top$ , run  $\tau$  on  $\varphi$  and prove resulting goals too

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$$\frac{\Gamma \vDash C[\top] \quad \Gamma' \vDash \varphi}{\Gamma \vDash C[\varphi]}$$

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$$\tau [(\Gamma', \varphi)] \rightarrow^* [(\Gamma_i, \varphi_i)]$$



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$$\frac{\frac{\Gamma \vDash C[\top] \quad \Gamma' \vDash \varphi}{\Gamma \vDash C[\varphi]} \quad \frac{\Gamma_i \vDash \varphi_i}{\Gamma' \vDash \varphi}}{\Gamma \vDash C[\varphi]} \quad \tau [(\Gamma', \varphi)] \rightarrow^* [(\Gamma_i, \varphi_i)]$$

- In a negative position: `with_tactic`  $\tau$   $\varphi \rightsquigarrow \varphi$

- Metaprograms, in general, perform correct transformations of the *proofstate*.

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- Basically a set of “goals” to be fulfilled

$$\Gamma_0 \vdash_{?_0} t_0$$

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$$\frac{\Gamma_1 \vdash^{?_1} : t_1 \quad \Gamma_2 \vdash^{?_2} : t_2 \quad \dots \quad \Gamma_n \vdash^{?_n} : t_n}{\Gamma_0 \vdash^{?_0} : t_0} R$$

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- The proofstate is transformed by primitives, which implement typing rules in backwards style
- Essentially scripting typing derivations instead of term syntax



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  - Completely standard and user-defined...
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  - ... except for the assumed primitives

`type error = exn * proofstate` (*\* error and proofstate at the time of failure \**)

`type result a = | Success : a → proofstate → result a | Failed : error → result a`

`let tac a = proofstate → Dv (result a)` (*\* Dv: possibly diverging \**)

`let t_return (x:α) = λps → Success x ps`

`let t_bind (m:tac α) (f:α → tac β) : tac β =`

`λps → match m ps with | Success x ps' → f x ps' | Error e → Error e`

`new_effect { TAC with repr = tac ; return = t_return ; bind = t_bind }`

`sub_effect DIV  $\rightsquigarrow$  TAC = ...`

`sub_effect EXN  $\rightsquigarrow$  TAC = ...`

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`sub_effect DIV  $\rightsquigarrow$  TAC = ...`

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- No put operation, can only modify proofstate via primitives:  
exact, apply, intro, tc, raise, catch, ...

Metaprograms are written as any other kind of program:

```
let mytac () : Tac unit =  
  let h1 = implies_intro () in  
  rewrite h1;  
  apply_lemma ('mylem);  
  ...
```

Higher-order combinators too:

```
let rec repeat (t : unit → Tac  $\alpha$ ) : Tac (list  $\alpha$ ) =  
  match catch t with  
  | Inl _ → []  
  | Inr x → x :: repeat t
```

```
let repeat1 (t : unit → Tac  $\alpha$ ) : Tac (list  $\alpha$ ) = t () :: repeat t
```

# TAC is a first-class citizen of $F^*$

Use exceptions:

```
exception NotAForall
```

```
let forall_intro () : Tac binder =  
  let g = cur_goal () in  
  match term_as_formula g with  
  | Forall _ _ → begin apply_lemma ('fa_intro_lem); intro () end  
  | _ → raise NotAForall
```

```
let t () =  
  try forall_intro () with  
  | NotAForall → ()  
  | e → raise e
```

# TAC is a first-class citizen of $F^*$

Call into existing pure, diverging, and exception-raising code:

```
let f (seen:list term) : Tac unit =  
  let g = cur_goal () in  
  if FStar.List.Tot.Base.existsb (term_eq g) seen then  
    raise Loop;  
  ...
```



## Customizing implicit arguments

Meta-F<sup>\*</sup> can also be used to provide strategies for resolution of implicits.

```
let diag (x:int) (#[same_as x] y : int) : int * int = (x, y)
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```
let diag (x:int) (#[same_as x] y : int) : int * int = (x, y)
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```
let _ = assert (diag 42 == (42, 42))
```

## Customizing implicit arguments

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```
let diag (x:int) (#[same_as x] y : int) : int * int = (x, y)
```

```
let _ = assert (diag 42 == (42, 42))
```

```
let _ = assert (diag 42 #21 == (42, 21))
```

# Putting it together: Typeclasses

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module FStar.Typeclasses
val mk_class : name → Tac unit (* creates method toplevels *)
val tcresolve : unit → Tac unit (* resolves dictionaries *)
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```
module MyMod
noeq type deq a = {
  eq : a → a → bool;
  eq_ok : (x:a) → (y:a) → Lemma (eq x y  $\iff$  x == y)
}
```

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```
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```

```
(* val eq : #a:Type → (#[tresolve] d : deq a) → (a → a → bool) *)
```

```
(* val eq_ok : #a:Type → (#[tresolve] d : deq a) → ((x:a) → (y:a) → Lemma ...) *)
```



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```
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```

```
module MyMod
```

```
class deq a = {
```

```
  eq : a → a → bool;
```

```
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```

```
}
```

```
(* val eq : #a:Type → ([#tcresolve] d : deq a) → (a → a → bool) *)
```

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[@tcinstance] let eq_int : deq int = { eq = ( $\lambda$  x y → x = y); eq_ok = easy }
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val mk_class : name → Tac unit (* creates method toplevels *)
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}
(* val eq : #a:Type → [| deq a |] → (a → a → bool) *)
(* val eq_ok : #a:Type → [| deq a |] → ((x:a) → (y:a) → Lemma ...) *)
instance eq_int : deq int = { eq = ( $\lambda$  x y → x = y); eq_ok = easy }
```

## A peek at tcresolve

```
let rec tcresolve' (seen:list term) (fuel:int) : Tac unit =
  if fuel ≤ 0 then
    fail "out of fuel";
  let g = cur_goal () in
  if FStar.List.Tot.Base.existsb (term_eq g) seen then
    fail "loop";
  let seen = g :: seen in
    local seen fuel 'or_else' global seen fuel
and local (seen:list term) (fuel:int) () : Tac unit =
  let bs = binders_of_env (cur_env ()) in
  first (λ b → trywith seen fuel (pack (Tv_Var (bv_of_binder b)))) bs
and global (seen:list term) (fuel:int) () : Tac unit =
  let cands = lookup_attr ('tinstance) (cur_env ()) in
  first (λ fv → trywith seen fuel (pack (Tv_FVar fv))) cands
and trywith (seen:list term) (fuel:int) (t:term) : Tac unit =
  (λ () → apply t) 'seq' (λ () → tcresolve' seen (fuel - 1))

let tcresolve () : Tac unit = tcresolve' [] 16
```

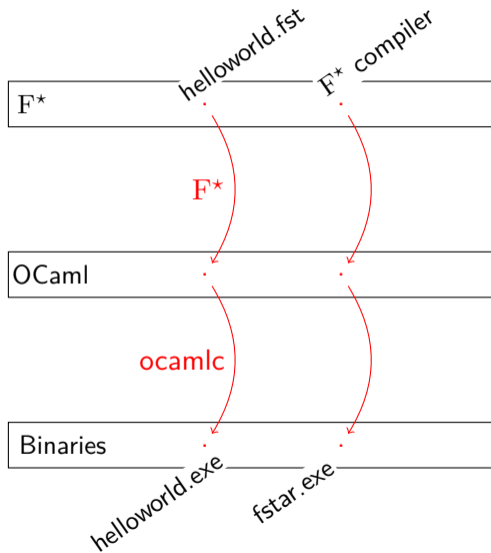
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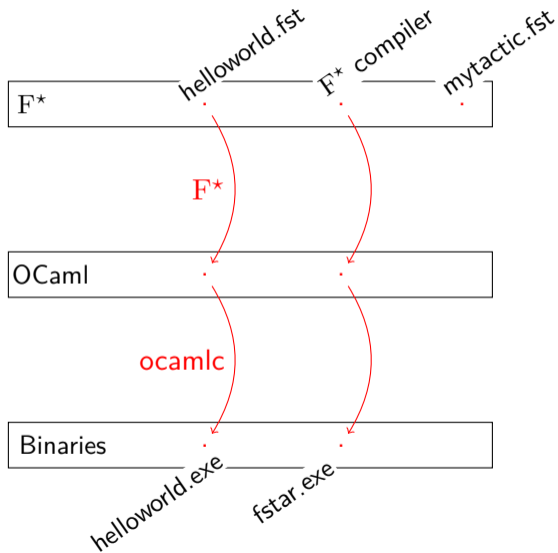
- By default, metaprograms are evaluated in  $F^*$ 's normalizer. Primitives are evaluated by calling into compiler internals.
- As an alternative, we can reuse  $F^*$ 's extraction mechanism to compile metaprograms as OCaml code.
- This code can then be compiled into dynamic objects and loaded



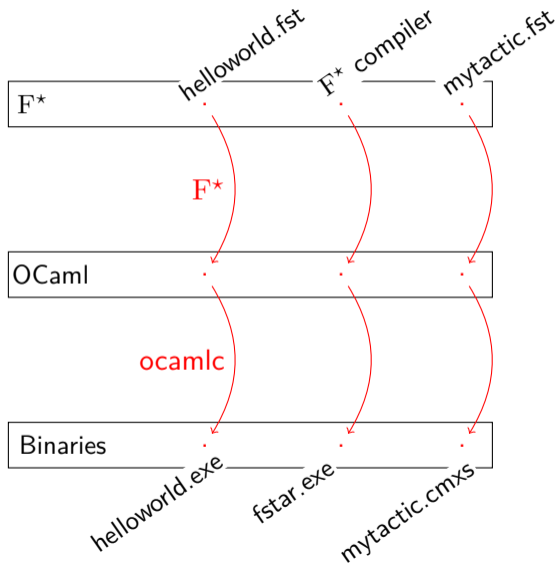
# Compilation



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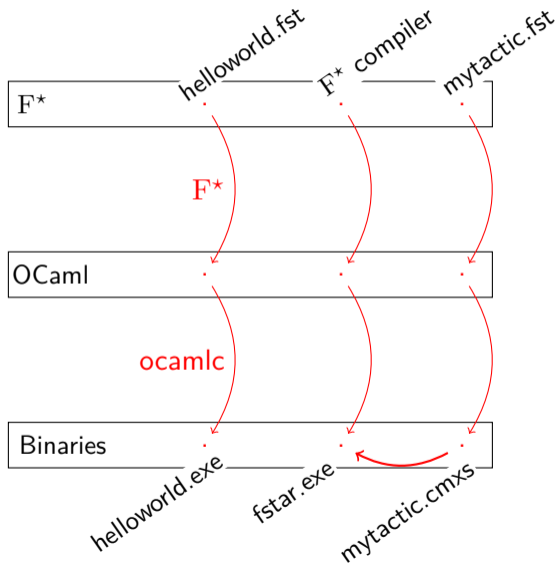


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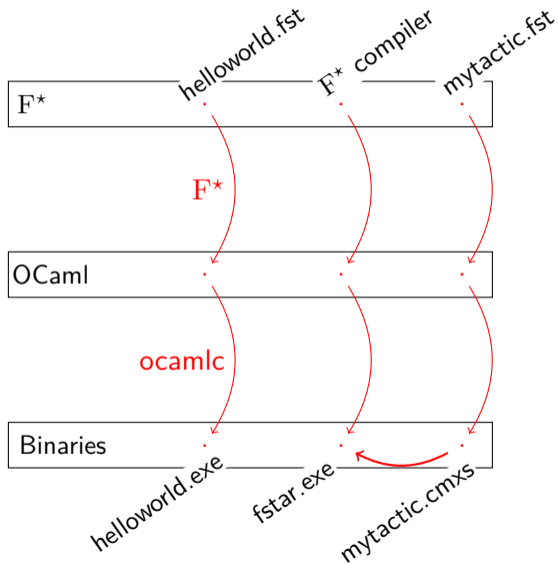
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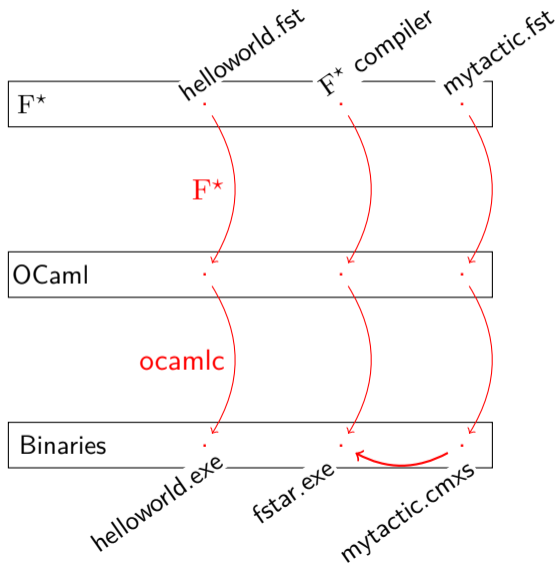
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- Not metaprogram specific *at all*

Coming back to this:

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let tresolve () = ...
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- `tresolve` outside of the TCB

# Summary

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- Using an effect for metaprograms increases reuse
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Thank you!

Goal 1/1

**p**: pos  
**n r h r0 r1 h0 \_h1 \_h2 s1 d0 d1 d2 h1 h2 hh**:  $\mathbb{Z}$   
**p**: pure\_post unit  
**uu\_\_\_**: squash ( $r_1 \geq 0 \wedge n > 0 \wedge 4 \times (n \times n) == p + 5 \wedge r == r_1 \times n + r_0 \wedge$   
 $h == h_2 \times (n \times n) + h_1 \times n + h_0 \wedge s_1 == r_1 + r_1 / 4 \wedge r_1 \% 4 == 0 \wedge d_0 == h_0 \times r_0 + h_1 \times s_1 \wedge$   
 $d_1 == h_0 \times r_1 + h_1 \times r_0 + h_2 \times s_1 \wedge d_2 == h_2 \times r_0 \wedge hh == d_2 \times (n \times n) + d_1 \times n + d_0 \wedge$   
 $(\forall (\text{pure\_result}: \text{unit}). h \times r \% p == hh \% p \implies p \text{ pure\_result}))$

**pure\_result**: unit

**uu\_\_\_**: squash ( $((h_2 \times r_0) \times (n \times n) + (h_0 \times ((r_1 / 4) \times 4) + h_1 \times r_0 + h_2 \times (5 \times (r_1 / 4)))) \times n +$   
 $(h_0 \times r_0 + h_1 \times (5 \times (r_1 / 4))) +$   
 $((h_2 \times n + h_1) \times (r_1 / 4)) \times p) \%$   
 $p =$   
 $((h_2 \times r_0) \times (n \times n) + (h_0 \times ((r_1 / 4) \times 4) + h_1 \times r_0 + h_2 \times (5 \times (r_1 / 4))) \times n +$   
 $(h_0 \times r_0 + h_1 \times (5 \times (r_1 / 4)))) \%$   
 $p)$

---

squash ( $4 \times (h_2 \times (n \times (n \times (n \times (r_1 / 4)))) + h_2 \times (n \times (n \times r_0)) +$   
 $(4 \times (n \times (n \times (h_1 \times (r_1 / 4)))) + n \times (h_1 \times r_0)) +$   
 $(4 \times (n \times (h_0 \times (r_1 / 4))) + h_0 \times r_0) ==$   
 $h_2 \times (n \times (n \times r_0)) + (4 \times (n \times (h_0 \times (r_1 / 4))) + n \times (h_1 \times r_0) + 5 \times (h_2 \times (n \times (r_1 / 4)))) +$   
 $(h_0 \times r_0 + 5 \times (h_1 \times (r_1 / 4))) +$   
 $(4 \times (h_2 \times (n \times (n \times (n \times (r_1 / 4)))) + -5 \times (h_2 \times (n \times (r_1 / 4)))) +$   
 $(4 \times (n \times (n \times (h_1 \times (r_1 / 4)))) + -5 \times (h_1 \times (r_1 / 4))))$

(\*?u3948\*) \_